New LDA formulation

#-----------------------------------------------------------

Based on Poisson-multinomial relationships, the above model is equivalent to:

This formulation is useful for us to calculate the log-likelihood. More specifically, we assume that:

Where

#-------------------------------------------

What if I sample betas using a Metropolis-Hastings algorithm but that relies on the expression above?